

**Problem 1: “A brief history” of life in the universe**

- 1-1.  $T = 10^{10} / (1)^{1/2} = 10^{10}$  K (10 billion degrees)
- 1-2.  $T = 10^{10} / (180)^{1/2} = 0.7 \times 10^9 \approx 10^9$  K (1 billion degrees)
- 1-3.  $t = [10^{10}/(3 \times 10^3)]^2 \text{ s} = 10^{13} \text{ s} = 3 \times 10^5 \text{ yr}$
- 1-4.  $t = (10^{10}/10^3)^2 \text{ s} = 10^{14} \text{ s} = 3 \times 10^6 \text{ yr}$
- 1-5. 100 K
- 1-6. 10 K
- 1-7. a - ( f ) - ( d ) - ( h ) - ( i ) - ( c ) - ( g ) - ( j ) - ( e ) - ( b )

**Problem 2: Hydrogen in outer space**

- 2-1.  $[(8 \times 8.3 \text{ J K}^{-1} \text{ mol}^{-1} \times 2.7 \text{ K}) / (3.14)(10^{-3} \text{ kg mol}^{-1})]^{1/2} = 240 \text{ m s}^{-1}$
- 2-2. volume of cylinder =  $(2)^{1/2} (3.14)(10^{-8} \text{ cm})^2 (2.4 \times 10^4 \text{ cm s}^{-1}) = 1.1 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1}$
- 2-3. collision/sec = (volume of cylinder) x (atoms/unit volume)  
 $= (1.1 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1})(10^{-6} \text{ cm}^{-3}) = 1.1 \times 10^{-17} \text{ s}^{-1}$   
time between collisions =  $1/(1.1 \times 10^{-17} \text{ s}^{-1}) = 9 \times 10^{16} \text{ s} = \text{about 3 billion yr}$
- 2-4.  $(240 \text{ m s}^{-1})(9 \times 10^{16} \text{ s}) = 2.2 \times 10^{19} \text{ m}$  (about 2,000 light yr)
- 2-5. Speed is proportional to the square root of the temperature.  
 $(240 \text{ m s}^{-1})(40/2.7)^{1/2} = 920 \text{ m s}^{-1}$
- 2-6. volume of cylinder =  $(2)^{1/2} (3.14)(10^{-8} \text{ cm})^2 (9.2 \times 10^4 \text{ cm s}^{-1}) = 4.1 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1}$   
collision/sec = (volume swept per second) x (atoms/unit volume)  
 $= (4.1 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1})(1 \text{ cm}^{-3}) = 4.1 \times 10^{-11} \text{ s}^{-1}$   
time between collisions =  $1/(4.1 \times 10^{-11} \text{ s}^{-1}) = 2.4 \times 10^{10} \text{ s} = \text{about 800 yr}$   
mean free path =  $(920 \text{ m s}^{-1})(2.4 \times 10^{10} \text{ s}) = 2.2 \times 10^{13} \text{ m}$   
 $\lambda$  (intergalactic space)/ $\lambda$ (interstellar space)  
 $= (2.2 \times 10^{19} \text{ m}) / (2.2 \times 10^{13} \text{ m}) = \text{about a million}$
- 2-7. very small

**Problem 3: Spectroscopy of interstellar molecules**

3-1.  $100\lambda = 2.9 \times 10^{-3} \text{ m K}$                        $\lambda = 2.9 \times 10^{-5} \text{ m}$   
 $E(\text{photon}) = hc/\lambda = (6.63 \times 10^{-34} \text{ J s}) (3.0 \times 10^8 \text{ m/s}) / (2.9 \times 10^{-5} \text{ m})$   
 $= 6.9 \times 10^{-21} \text{ J}$

3-2. J:  $0 \leftrightarrow 1$   
 $\mu = (12 \times 16 / 28)(1.66 \times 10^{-27} \text{ kg}) = 1.14 \times 10^{-26} \text{ kg}$   
 $I = \mu R^2 = (1.14 \times 10^{-26} \text{ kg})(1.13 \times 10^{-10} \text{ m})^2 = 1.45 \times 10^{-46} \text{ kg m}^2$   
 $E(0 \leftrightarrow 1) = 2 h^2 / 8\pi^2 I = 2(6.63 \times 10^{-34} \text{ J s})^2 / [8\pi^2 (1.45 \times 10^{-46} \text{ kg m}^2)]$   
 $= 7.68 \times 10^{-23} \text{ J}$   
 $E(\text{photon}) \text{ of Problem 3-1} = 6.9 \times 10^{-21} \text{ J} > E(0 \leftrightarrow 1) = 7.68 \times 10^{-23} \text{ J}$   
 Rotational excitation by the background radiation is feasible.

3-3.  $E(0 \leftrightarrow 2) = 6 h^2 / 8\pi^2 I = hc/\lambda$                        $\lambda = 8\pi^2 c I / 6h$   
 $I = \mu R^2 = [(1/2) \times 1.66 \times 10^{-27} \text{ kg}](0.74 \times 10^{-10} \text{ m})^2 = 4.55 \times 10^{-48} \text{ kg m}^2$   
 $\lambda = 8\pi^2 c I / 6h$   
 $= [8\pi^2 \times 4.55 \times 10^{-48} \text{ kg m}^2 \times 3 \times 10^8 \text{ m/s}] / (6 \times 6.63 \times 10^{-34} \text{ J s})$   
 $= 2.71 \times 10^{-5} \text{ m}$   
 $T = 2.9 \times 10^{-3} \text{ m K} / \lambda = 2.9 \times 10^{-3} \text{ m K} / 2.71 \times 10^{-5} \text{ m} = 107 \text{ K}$   
 Observation of hydrogen rotational spectra is feasible at 100 K.

**Problem 4: Ideal gas law at the core of the sun**

4-1. protons:  $(158 \text{ g/cm}^3 \times 0.36) / (1.0 \text{ g/mole}) = 57 \text{ mol/cm}^3$   
 helium nuclei:  $(158 \text{ g/cm}^3 \times 0.64) / (4.0 \text{ g/mole}) = 25 \text{ mol/cm}^3$   
 electrons:  $57 + (25 \times 2) = 107 \text{ mol/cm}^3$   
 Total:  $189 \text{ mol/cm}^3$

4-2. volume of a hydrogen molecule =  $2 (4/3) \pi r^3$   
 $= 2 \times (4/3) \pi \times (0.53 \times 10^{-8} \text{ cm})^3 = 1.2 \times 10^{-24} \text{ cm}^3$   
 hydrogen gas:  $V/n = RT/p = (0.082 \text{ atm L K}^{-1} \text{ mol}^{-1}) \times 300 \text{ K} / 1 \text{ atm}$   
 $= 24.6 \text{ L/mole} = 4.1 \times 10^{-23} \text{ L/molecule} = 4.1 \times 10^{-20} \text{ cm}^3/\text{molecule}$

$$1.2 \times 10^{-24} \text{ cm}^3 / 4.1 \times 10^{-20} \text{ cm}^3 = 3 \times 10^{-5} = 0.003 \%$$

$$\begin{aligned} \text{liquid hydrogen: } & (2 \text{ g/mole}) / (0.09 \text{ g/cm}^3) / (6 \times 10^{23} \text{ molecule /mole}) \\ & = 3.7 \times 10^{-23} \text{ cm}^3 \end{aligned}$$

$$(1.2 \times 10^{-24} \text{ cm}^3) / (3.7 \times 10^{-23} \text{ cm}^3) = 0.03 = 3 \%$$

solar plasma: neglect volume of electrons

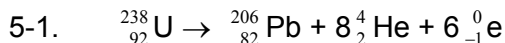
$$\begin{aligned} & (4/3)(\pi)(1.4 \times 10^{-13} \text{ cm})^3 (1 \times 57 \text{ mol/cm}^3 + 4 \times 25 \text{ mol/cm}^3)(6 \times 10^{23} \text{ mol}^{-1}) \\ & = 1.1 \times 10^{-12} = 1 \times 10^{-10} \% \end{aligned}$$

Volume occupied is extremely small and ideal gas law is applicable.

4-3. From 4-1, we know there are 189 moles of particles/cm<sup>3</sup>.

$$T = pV/nR = (2.5 \times 10^{11})(1 \times 10^{-3}) / (189)(0.082) = 1.6 \times 10^7 \text{ K}$$

### Problem 5: Atmosphere of the planets



5-2. After almost one half-life, the molar ratio between Pb-206 and U-238 is 1.

$$\text{Mass ratio: Pb-206/U-238} = 206/238 = 0.87$$

$$5-3. \quad (1/2)mv_e^2 = GMm/R$$

$$v_e^2 = (2GM/R) = [(2)(6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2})(5.98 \times 10^{24} \text{ kg}) / (6.37 \times 10^6 \text{ m})]$$

$$v_e = 1.12 \times 10^4 \text{ m s}^{-1}$$

$$5-4. \quad \text{hydrogen atom: } (8RT/\pi M)^{1/2}$$

$$= [(8)(8.3145 \text{ kg m}^2 \text{ s}^{-2} \text{ mol}^{-1} \text{ K}^{-1})(298 \text{ K}) / (3.14)(1.008 \times 10^{-3} \text{ kg mol}^{-1})]^{1/2}$$

$$= 2500 \text{ m s}^{-1} \text{ (22\% of the escape velocity)}$$

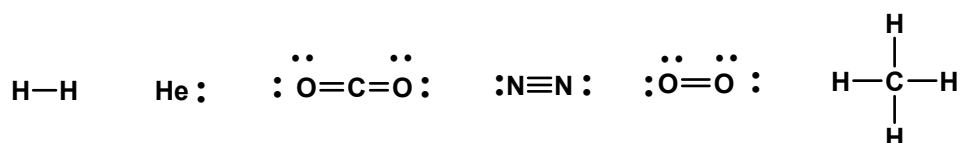
nitrogen molecule:

$$2500 \text{ m s}^{-1} \times (1/28)^{1/2} = 470 \text{ m s}^{-1} \text{ (4\% of the escape velocity)}$$

The fraction with speed exceeding the escape velocity is much greater for hydrogen atoms than for nitrogen molecules.

- 5-5. a. Jupiter: large mass, low temperature, H/He retained at high pressure  
 b. Venus: lost light elements, rich in carbon dioxide, high pressure  
 c. Mars: small mass, rich in carbon dioxide, low pressure  
 d. Earth: lost light elements, carbon dioxide converted to oxygen  
     through photosynthesis  
 e. Pluto: very small mass, lost light elements, very low atmospheric pressure

5-6.



- 5-7. He (4K) < H<sub>2</sub> (20K) < N<sub>2</sub> (77K) < O<sub>2</sub> (90K) < CH<sub>4</sub> (112K)  
 Dispersion force is greater for larger molecules.  
 Nitrogen with the triple bond has a smaller bond length than oxygen.  
 Nitrogen also has less lone pair electrons to be involved in dispersion.

### Problem 6: Discovery of the noble gases

- 6-1. In 1816 Prout published a hypothesis that all matter is composed ultimately of hydrogen. (Later, Harlow Shapley, an eminent astronomer, said that if God did create the world by a word, the word would have been hydrogen.) Prout cited as evidence the fact that the specific gravities of gaseous elements appeared to be whole-number multiples of the value for hydrogen.
- 6-2.  $28 \text{ NH}_3 + 21 \text{ O}_2 + 78 \text{ N}_2 + \text{Ar} \rightarrow 92 \text{ N}_2 + 42 \text{ H}_2\text{O} + \text{Ar}$
- 6-3.  $[(92)(2)(14.0067) + 39.948]/93 = 28.142$
- 6-4.  $78 \text{ N}_2 + 21 \text{ O}_2 + \text{Ar} + 42 \text{ Cu} \rightarrow 78 \text{ N}_2 + 42 \text{ CuO} + \text{Ar}$
- 6-5.  $[(78)(2)(14.0067) + 39.948]/79 = 28.164$

- 6-6.  $28.164/28.142 = 1.0008$  (about 0.1%)
- 6-7.  $4 \text{ NH}_3 + 3 \text{ O}_2 \rightarrow 2 \text{ N}_2 + 6 \text{ H}_2\text{O}$   
 Molecular weight of pure nitrogen =  $(2)(14.0067) = 28.013$   
 $28.164/28.013 = 1.0054$   
 The discrepancy would increase about 7-fold ( $0.0054/0.0008$ ).
- 6-8.  $40/29 = 1.4$
- 6-9.  $5R/3R = 1.67$  translational
- 6-10. volume of air =  $1000 \text{ m}^3 = 10^6$  liter  
 $(10^6)/22.4 = 4.5 \times 10^4$  mol of air  
 weight of argon =  $(4.5 \times 10^4)(0.01)(40) = 1.8 \times 10^4 \text{ g} = 18 \text{ kg}$
- 6-11. helium - sun  
 neon - new  
 argon - lazy  
 krypton - hidden  
 xenon - stranger

### Problem 7: Solubility of salts

- 7-1.  $\text{AgCl}(s) \rightarrow \text{Ag}^+(aq) + \text{Cl}^-(aq)$   
 $K_{sp} = [\text{Ag}^+][\text{Cl}^-] = x^2 = 1.8 \times 10^{-10} \Rightarrow [\text{Ag}^+] = [\text{Cl}^-] = 1.34 \times 10^{-5} \text{ M}$
- $\text{AgBr}(s) \rightarrow \text{Ag}^+(aq) + \text{Br}^-(aq)$   
 $K_{sp} = [\text{Ag}^+][\text{Br}^-] = x^2 = 3.3 \times 10^{-13} \Rightarrow [\text{Ag}^+] = [\text{Br}^-] = 5.74 \times 10^{-7} \text{ M}$
- 7-2. In this hypothetical case,  $[\text{Ag}^+] = [\text{Cl}^-] = 1.34 \times 10^{-5} \text{ M}$  just as in 7-1.  
 $\text{Cl}^-(aq)/\text{Cl}(\text{total}) = \text{Cl}^-(aq)/(\text{Cl}^-(aq) + \text{AgCl}(s))$   
 $= (1.3 \times 10^{-5} \text{ M})(0.200 \text{ L})/1.00 \times 10^{-4} \text{ mol} = 0.027 = 2.7\%$

7-3. Similarly,  $[Ag^+] = [Br^-] = 5.7_4 \times 10^{-7} \text{ M}$  just as in 7-1.

$$\begin{aligned} Br^-(aq)/Br(\text{total}) &= Br^-(aq)/(Br^-(aq)+AgBr(s)) \\ &= (5.7 \times 10^{-7} \text{ M})(0.200 \text{ L})/1.00 \times 10^{-4} \text{ mol} = 1.1 \times 10^{-3} = 0.11\% \end{aligned}$$

7-4. Assume that  $1.00 \times 10^{-4} \text{ mol}$  of  $AgCl$  is precipitated, and  $1.00 \times 10^{-6} \text{ mol}$  of  $Ag^+$  ion remains in solution. Then a portion of  $AgCl$  dissolves.

$$\begin{aligned} [Ag^+] &= 5.0 \times 10^{-6} + x, [Cl^-] = x \\ K_{sp} &= [Ag^+][Cl^-] = (5.0 \times 10^{-6} + x)(x) = 1.8 \times 10^{-10} \\ \Rightarrow [Cl^-] &= 1.1 \times 10^{-5} \text{ M (slightly decreased)} \\ [Ag^+] &= 1.6 \times 10^{-5} \text{ M (slightly increased)} \\ Cl^-(aq)/Cl(\text{total}) &= Cl^-(aq)/(Cl^-(aq)+AgCl(s)) \\ &= (1.1 \times 10^{-5} \text{ M})(0.200 \text{ L})/1.00 \times 10^{-4} \text{ mol} = 0.022 = 2.2\% \end{aligned}$$

Similarly,

$$\begin{aligned} [Ag^+] &= 5.0 \times 10^{-6} + x, [Br^-] = x \\ K_{sp} &= [Ag^+][Br^-] = (5.0 \times 10^{-6} + x)(x) = 3.3 \times 10^{-13} \\ x < 5.0 \times 10^{-6}; \text{ therefore, } &(5.0 \times 10^{-6})(x) = 3.3 \times 10^{-13} \\ \Rightarrow [Br^-] &= 6.6 \times 10^{-8} \text{ M (significant decrease from } 5.7 \times 10^{-7} \text{ M)} \\ [Ag^+] &= 5.1 \times 10^{-6} \text{ M (significant increase from } 5.7 \times 10^{-7} \text{ M)} \\ Br^-(aq)/Br(\text{total}) &= Br^-(aq)/(Br^-(aq)+AgBr(s)) \\ &= (6.5 \times 10^{-8} \text{ M})(0.200 \text{ L})/1.00 \times 10^{-4} \text{ mol} = 1.3 \times 10^{-4} = 0.013\% \end{aligned}$$

7-5.  $AgBr$  will precipitate first. Theoretically,  $AgBr$  will begin to precipitate when the  $Ag^+$  concentration reaches  $3.3 \times 10^{-10} \text{ M}$ . At this concentration of  $Ag^+$ ,  $AgCl$  will not precipitate.

$$AgBr: [Ag^+] = K_{sp}/[Br^-] = 3.3 \times 10^{-13}/1.0 \times 10^{-3} = 3.3 \times 10^{-10} \text{ M}$$

This corresponds to  $3.3 \times 10^{-8} \text{ L}$  of the  $Ag^+$  solution, which is much less than the smallest volume one can deliver with a micropipet.

7-6. This problem can be solved using the mass conservation relations. Or the solution can be simplified as shown below.

$$A = \text{total amount of Ag} = [\text{Ag}^+]_0 V_{\text{add}} = (1.00 \times 10^{-3} \text{ M}) V_{\text{add}}$$

$$B = \text{total amount of Br} = [\text{Br}^-]_0 V_{\text{original}} = (1.00 \times 10^{-3} \text{ M})(0.100 \text{ L}) = 1.00 \times 10^{-4} \text{ mol}$$

$$C = \text{total amount of Cl} = [\text{Cl}^-]_0 V_{\text{original}} = (1.00 \times 10^{-3} \text{ M})(0.100 \text{ L}) = 1.00 \times 10^{-4} \text{ mol}$$

$$A = [\text{Ag}^+] V_{\text{tot}} + n_{\text{AgCl(s)}} + n_{\text{AgBr(s)}} \quad (1)$$

$$B = [\text{Br}^-] V_{\text{tot}} + n_{\text{AgBr(s)}} \quad (2)$$

$$C = [\text{Cl}^-] V_{\text{tot}} + n_{\text{AgCl(s)}} \quad (3)$$

$$K_{\text{sp}}(\text{AgBr}) = [\text{Ag}^+][\text{Br}^-] \quad (4)$$

$$K_{\text{sp}}(\text{AgCl}) = [\text{Ag}^+][\text{Cl}^-] \quad (5)$$

►  $V_{\text{add}} = 100 \text{ mL}$ ,  $V_{\text{tot}} = 200 \text{ mL}$  (total Ag =  $1.00 \times 10^{-4} \text{ mol}$ )

Assume that all  $\text{Ag}^+$  are used to precipitate  $\text{Br}^-$  as  $\text{AgBr(s)}$ .

$$[\text{Ag}^+] = [\text{Br}^-] = 0, [\text{Cl}^-] = 5.0 \times 10^{-4} \text{ M}, \text{AgBr} = 1.00 \times 10^{-4} \text{ mol}, \text{AgCl} = 0$$

At equilibrium,

$$[\text{Ag}^+] = K_{\text{sp}}(\text{AgCl})/[\text{Cl}^-] = 3.6 \times 10^{-7} \text{ M}$$

$$[\text{Br}^-] = K_{\text{sp}}(\text{AgBr})/[\text{Ag}^+] = 9.2 \times 10^{-7} \text{ M}$$

$$\text{total Ag} = \text{Ag}^+(\text{aq}) + \text{AgBr} + \text{AgCl}, \text{total Br} = \text{Br}^-(\text{aq}) + \text{AgBr}$$

$$\text{Since total Ag} = \text{total Br}, \text{Ag}^+(\text{aq}) + \text{AgCl} = \text{Br}^-(\text{aq})$$

$$\text{AgCl} = ([\text{Br}^-] - [\text{Ag}^+])V_{\text{tot}} = [(9.2 - 3.6) \times 10^{-7} \text{ M}](0.200 \text{ L})$$

$$= 1.1 \times 10^{-7} \text{ mol} \text{ (0.11\% of the total Cl)}$$

$$[\text{Cl}^-] = 5.0 \times 10^{-4} \text{ M} \text{ (still valid, because very little AgCl is formed)}$$

$$\text{AgBr} = 1.00 \times 10^{-4} \text{ mol} \text{ (still valid, because } [\text{Br}^-] \text{ is small)}$$

►  $V_{\text{add}} = 200 \text{ mL}$ ,  $V_{\text{tot}} = 300 \text{ mL}$  (total Ag =  $2.00 \times 10^{-4} \text{ mol}$ )

Assume complete precipitation of  $\text{Br}^-$  and  $\text{Cl}^-$  with  $\text{Ag}^+$

$$[\text{Ag}^+] = [\text{Br}^-] = [\text{Cl}^-] = 0, \text{AgBr} = 1.0 \times 10^{-4} \text{ mol}, \text{AgCl} = 1.0 \times 10^{-4} \text{ mol}$$

At equilibrium,

$$[\text{Ag}^+] = [\text{Br}^-] + [\text{Cl}^-] = K_{\text{sp}}(\text{AgCl})/[\text{Ag}^+] + K_{\text{sp}}(\text{AgBr})/[\text{Ag}^+]$$

$$[\text{Ag}^+] = 1.3 \times 10^{-5} \text{ M}$$

$$[\text{Br}^-] = K_{\text{sp}}(\text{AgBr}) / [\text{Ag}^+] = 2.5 \times 10^{-8} \text{ M}$$

$$[\text{Cl}^-] = K_{\text{sp}}(\text{AgCl}) / [\text{Ag}^+] = 1.3 \times 10^{-5} \text{ M}$$

$$\text{AgBr} = 1.00 \times 10^{-4} \text{ mol} - [\text{Br}^-]V_{\text{tot}} = 1.00 \times 10^{-4} \text{ mol}$$

$$\text{AgCl} = 1.00 \times 10^{-4} \text{ mol} - [\text{Cl}^-]V_{\text{tot}} = 9.6 \times 10^{-5} \text{ mol}$$

►  $V_{\text{add}} = 300 \text{ mL}$ ,  $V_{\text{tot}} = 400 \text{ mL}$  (total Ag =  $3.00 \times 10^{-4} \text{ mol}$ )

Assume complete precipitation of  $\text{Br}^-$  and  $\text{Cl}^-$  with  $\text{Ag}^+$ .

$$[\text{Ag}^+] = 2.5 \times 10^{-4} \text{ M}, [\text{Br}^-] = [\text{Cl}^-] = 0, \text{AgBr} = 1.0 \times 10^{-4} \text{ mol}, \text{AgCl} = 1.0 \times 10^{-4} \text{ mol}$$

$$[\text{Br}^-] = K_{\text{sp}}(\text{AgBr})/[\text{Ag}^+] = 1.3 \times 10^{-9} \text{ M}$$

$$[\text{Cl}^-] = K_{\text{sp}}(\text{AgCl})/[\text{Ag}^+] = 7.2 \times 10^{-7} \text{ M}$$

$$\text{AgBr} = 1.00 \times 10^{-4} \text{ mol} - [\text{Br}^-]V_{\text{tot}} = 1.00 \times 10^{-4} \text{ mol}$$

$$\text{AgCl} = 1.00 \times 10^{-4} \text{ mol} - [\text{Cl}^-]V_{\text{tot}} = 9.97 \times 10^{-5} \text{ mol}$$

$V_{\text{add}}$	% Br in solution	% Br in precipitate	% Cl in solution	% Cl in precipitate	% Ag in solution	% Ag in precipitate
100 mL	0.18	99.8	99.9	0.11	0.07	99.9
200 mL	0.007	100	4.0	96	2.0	98.0
300 mL	0.0005	100	0.3	99.7	33.3	66.7

### Problem 8: Physical methods for determination of Avogadro's number

8-1. (a) volume of particle =  $(4 \times 3.14/3)(0.5 \times 10^{-6}/2)^3 \text{ m}^3 = 6.54 \times 10^{-14} \text{ cm}^3$   
 effective mass =  $(6.54 \times 10^{-14} \text{ cm}^3)(1.10 - 1.00) \text{ g/cm}^3 = 6.54 \times 10^{-15} \text{ g}$

(b)  $mg(h - h_0)/k_B T = 1$

$$k_B = (6.54 \times 10^{-18} \text{ kg})(9.81 \text{ m s}^{-2})(6.40 \times 10^{-5} \text{ m})/293.15 \text{ K}$$

$$= 1.40 \times 10^{-23} \text{ J K}^{-1}$$

(c) Avogadro's number =  $R/k_B$

$$= (8.314 \text{ J mol}^{-1} \text{ K}^{-1})/(1.40 \times 10^{-23} \text{ J K}^{-1}) = 5.94 \times 10^{23} \text{ mol}^{-1}$$

8-2. Length of the edge of a unit cell =  $2 \times 2.819 \times 10^{-8} \text{ cm} = 5.638 \times 10^{-8} \text{ cm}$

$$\text{volume of a unit cell} = (5.638 \times 10^{-8} \text{ cm})^3 = 1.792 \times 10^{-22} \text{ cm}^3$$

$$\text{volume per Na}^+ \text{ plus Cl}^- = 1.792 \times 10^{-22} \text{ cm}^3 / 4 = 4.480 \times 10^{-23} \text{ cm}^3$$

$$\text{formula weight of NaCl} = 22.99 + 35.45 = 58.44$$

$$\text{molar volume of the crystal} = 58.44 \text{ g} / 2.165 \text{ g cm}^{-3} = 26.99 \text{ cm}^3$$

$$\text{Avogadro's number} = (26.99 \text{ cm}^3) / (4.480 \times 10^{-23} \text{ cm}^3) = 6.025 \times 10^{23}$$

8-3. Avogadro's number =  $96496 \text{ C} / 1.593 \times 10^{-19} \text{ C} = 6.058 \times 10^{23}$



**Problem 9: An electrochemical method for determination of Avogadro's number**

- 9-1. anode:  $\text{Cu(s)} \rightarrow \text{Cu}^{2+}(\text{aq}) + 2 \text{e}^-$ ; cathode :  $2 \text{H}^+(\text{aq}) + 2 \text{e}^- \rightarrow \text{H}_2(\text{g})$
- 9-2. total charge =  $(0.601 \text{ A})(1 \text{ C s}^{-1}/1 \text{ A})(1802 \text{ s}) = 1083 \text{ C}$
- 9-3. number of electrons =  $(1083 \text{ C})(1 \text{ electron}/1.602 \times 10^{-19} \text{ C}) = 6.760 \times 10^{21}$
- 9-4. number of copper atoms =  $(6.760 \times 10^{21})/2 = 3.380 \times 10^{21}$   
mass of a copper atom =  $0.3554 \text{ g}/3.380 \times 10^{21} = 1.051 \times 10^{-22} \text{ g}$
- 9-5. Avogadro's number =  $63.546 \text{ g}/1.051 \times 10^{-22} \text{ g} = 6.046 \times 10^{23}$
- 9-6. Percent error:  $(6.046 \times 10^{23} - 6.022 \times 10^{23})/(6.022 \times 10^{23}) = 0.4 \%$
- 9-7. Weight of  $\text{H}_2$  evolved =  $(1 \text{ g})(6.760 \times 10^{21}/6.02 \times 10^{23}) = 0.011 \text{ g}$   
Collecting and weighing such a small amount of any gas is not practical considering buoyancy correction.

**Problem 10: Enthalpy, entropy, and stability**

- 10-1. (a)  $K_{\text{eq}}$  and  $\Delta G$  (b)  $\Delta H$  (c)  $\Delta S$  (d)  $K_{\text{eq}}$  (e)  $\Delta G$  (f)  $\Delta H$
- 10-2. From  $\Delta G = -RT \ln K_p$ ,  $\Delta G$  is 1.52 kcal/mol for  $\text{Me}_3\text{P} \cdot \text{BMe}_3$  and 0.56 kcal/mol for  $\text{Me}_3\text{N} \cdot \text{BMe}_3$ .  $\text{Me}_3\text{P} \cdot \text{BMe}_3$  is more stable (less likely to dissociate) than  $\text{Me}_3\text{N} \cdot \text{BMe}_3$  at 100 °C.
- 10-3.  $\Delta G = \Delta H - T\Delta S$   
 $\Delta H_{373} = \Delta G_{373} + 373 \Delta S_{373} \approx \Delta G_{373} + 373 \Delta S^\circ$ ,  
 $\text{Me}_3\text{N} \cdot \text{BMe}_3$  :  $\Delta H = 0.56 \text{ kcal/mol} + (373 \text{ K})(45.7 \text{ cal/mol} \cdot \text{K}) = 17.6 \text{ kcal/mol}$   
 $\text{Me}_3\text{N} \cdot \text{PMe}_3$  :  $\Delta H = 1.52 \text{ kcal/mol} + (373 \text{ K})(40.0 \text{ cal/mol} \cdot \text{K}) = 16.4 \text{ kcal/mol}$

More heat is needed to dissociate  $\text{Me}_3\text{N}\cdot\text{BMe}_3$ . Therefore, the N-B central bond is stronger.

10-4.  $\text{Me}_3\text{N}\cdot\text{BMe}_3$  :

$$\Delta H = 17.6 \text{ kcal/mol} \quad - T\Delta S = - (373)(45.7) = -17.05 \text{ kcal/mol}$$

$$\Delta G = 0.56 \text{ kcal/mol}$$

$\text{Me}_3\text{P}\cdot\text{BMe}_3$  :

$$\Delta H = 16.4 \text{ kcal/mol} \quad - T\Delta S = - (373)(40.0) = -14.92 \text{ kcal/mol}$$

$$\Delta G = 1.52 \text{ kcal/mol}$$

Enthalpy change is larger for  $\text{Me}_3\text{N}\cdot\text{BMe}_3$ ; however, larger increase in the entropy term leads to a smaller increase in Gibbs free energy for  $\text{Me}_3\text{N}\cdot\text{BMe}_3$ .

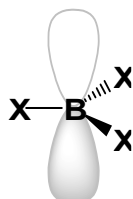
10-5.  $17600 \text{ cal/mol} - (45.7 \text{ cal/mol}\cdot\text{K}) T > 16400 \text{ cal/mol} - (40.0 \text{ cal/mol}\cdot\text{K}) T$

$$5.7 \text{ (cal/mol}\cdot\text{K}) T < 1200 \text{ cal/mol}$$

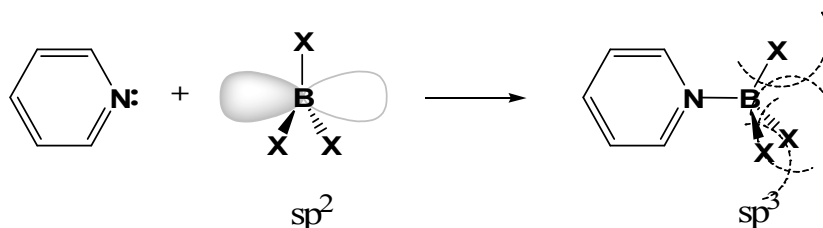
$$T < 210\text{K} (-63^\circ\text{C})$$

### Problem 11: Lewis acids and bases

11-1. Central B has  $sp^2$  hybridization and  $\text{BX}_3$  is triangular.



11-2. When an adduct is formed with pyridine, the structure around the central boron becomes tetragonal  $sp^3$  hybrid type (tetrahedron) structure. This structural change will induce steric hindrance around boron which is more pronounced with larger groups (i.e., iodines) and adduct formation is not preferred. Therefore,  $\text{BF}_3$  is predicted to show the greatest preference to form adduct. ( $\text{BF}_3$  is expected to show the strongest Lewis acidity)



- 11-3. The more electronegative halogen is expected to effectively remove electron density from the central boron and increase acidity.

Lewis acidity:  $\text{BF}_3 > \text{BCl}_3 > \text{BBr}_3$

- 11-4. Like neutralization that occurs between HCl and NaOH, the reaction producing stable acid-base adduct is expected to be exothermic. The enthalpy change will be the largest for the strongest Lewis acid,  $\text{BF}_3$ .

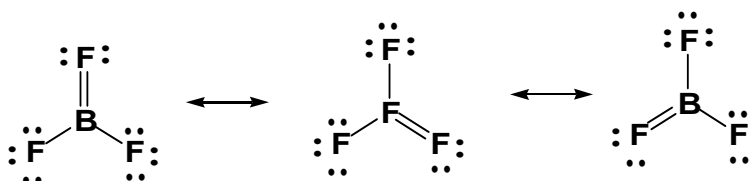
- 11-5.
- |   |               |                |                |            |
|---|---------------|----------------|----------------|------------|
|   | $\text{BF}_3$ | $\text{BCl}_3$ | $\text{BBr}_3$ |            |
| $\Delta H_3 = \Delta H_1 + \Delta H_2;$ | - 31.7        | - 39.5         | - 44.5         | (kcal/mol) |

The actual order of acidity is opposite from prediction based on the electronegativity of the halides.

- 11-6. A =  $\text{BF}_3 \cdot \text{H}_2\text{O}$   
 B =  $\text{B}(\text{OH})_3$ , C = 3 HX (3 HCl or 3 HBr)

Strong Lewis acids such as  $\text{BCl}_3$  and  $\text{BBr}_3$  can activate O-H bonds in  $\text{H}_2\text{O}$  molecule to produce  $\text{B}(\text{OH})_3$  by releasing HX. Dative  $\pi$ -bonding with lone pair electrons of O, which have a similar energy level, can stabilize  $\text{B}(\text{OH})_3$  as explained in 11-7.

- 11-7. Empty  $p_z$ -orbital in boron can accept a dative  $\pi$ -bond from the lone pair electrons of fluorine, which satisfies the 'octet rule' for boron and shortens the boron-fluorine bond distance.



Since resonance structures of this kind are not possible in the adduct compounds, effective resonance will reduce the tendency for pyridine adduct formation.

The ability to form dative  $\pi$ -bonding appears to decrease sharply in the heavier elements due to the energy differences between B and X. Resonance of this dative  $\pi$ -bonding should be of lesser importance in the chloride and least importance in the bromide. These resonance structures having dative  $\pi$ -bonding are sufficiently large so as to reverse the trend expected from the relative inductive effects and the steric effects from the adduct formations.

### Problem 12: Solubility equilibrium in a buffer solution

12-1. 440 mL H<sub>2</sub>S in 100 mL of water = 4.4 L H<sub>2</sub>S in 1 L of water = 0.20 M

12-2. For approximation, the concentration of all anions in (5) except [Cl<sup>-</sup>], which is 0.02, can be crossed out. Thus (5) becomes

$$[\text{H}^+] + 2[\text{Fe}^{2+}] = [\text{Cl}^-] = 0.020 \quad (6)$$

$$\text{Combine (2) and (3): } [\text{H}^+]^2 [\text{S}^{2-}]/[\text{H}_2\text{S}] = 1.24 \times 10^{-21}$$

$$\text{Since } [\text{H}_2\text{S}] = 0.2, \text{ one gets } [\text{H}^+]^2 [\text{S}^{2-}] = 2.48 \times 10^{-22} \quad (7)$$

$$\text{Combine (1) and (7): } [\text{H}^+]^2 (8.0 \times 10^{-19}/[\text{Fe}^{2+}]) = 2.48 \times 10^{-22}$$

$$[\text{H}^+]^2 = 3.1 \times 10^{-4} [\text{Fe}^{2+}] \quad (8)$$

Combine (6) and (8) and solve for [H<sup>+</sup>]:

$$[\text{H}^+] = 0.0176 \quad \text{pH} = 1.75$$

$$[\text{Fe}^{2+}] = (0.020 - 0.0176)/2 = 0.0012 \text{ (12\% remains in solution)}$$

$$\text{Check: } [\text{HS}^-] = (9.5 \times 10^{-8})[\text{H}_2\text{S}]/[\text{H}^+] = 1.1 \times 10^{-6} \ll [\text{Cl}^-] = 0.02$$

$$[\text{S}^{2-}] = (1.3 \times 10^{-14})[\text{HS}^-]/[\text{H}^+] = 2.5 \times 10^{-18}$$

$$[\text{OH}^-] = 5.7 \times 10^{-13}$$

Eq. (8) shows that 10-fold decrease in [H<sup>+</sup>] increases [Fe<sup>2+</sup>] 180-fold.

12-3. From  $[H^+]^2 = 3.1 \times 10^{-4} [Fe^{2+}]$ ,  
 $[H^+] = [(3.1 \times 10^{-4})(1 \times 10^{-8})]^{1/2} = 1.76 \times 10^{-6}$                       pH = 5.75

12-4. original HOAc = 0.10 M x 100 mL = 10 mmol  
 Henderson-Hasselbalch eq for the HOAc-OAc<sup>-</sup> buffer at pH 5.75  
 $pH = 5.75 = pK + \log [OAc^-]/[HOAc] = 4.74 + \log [OAc^-]/[HOAc]$   
 initial Fe<sup>2+</sup> = 0.01 M x 100 mL = 1 mmol  
 H<sup>+</sup> produced upon precipitation of 1 mmol Fe<sup>2+</sup> = 2 mmol  
 OAc<sup>-</sup> consumed by H<sup>+</sup> produced = 2 mmol  
 $\log [OAc^-]/[HOAc] = 5.75 - 4.74 = 1.01$   
 Let x = original mmol OAc<sup>-</sup>  
 $(x - 2)/(10 + 2) = 10^{1.01} = 10.2$ , x = 124 mmol  
 $[OAc^-] = 124 \text{ mmol}/100 \text{ mL} = 1.24 \text{ M}$

12-5. pH = 4.74 + log (1.24/0.10) = 5.83

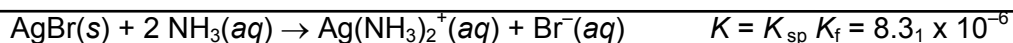
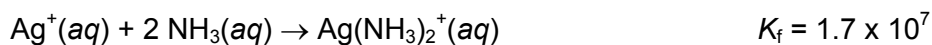
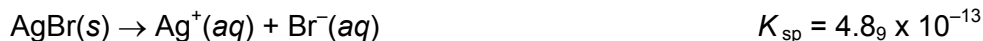
### Problem 13: Redox potential, Gibbs free energy, and solubility

13-1.  $Ag^+(aq) + e^- \rightarrow Ag(s)$      $E^\circ = 0.7996 \text{ V}$   
 $\Delta G^\circ = \Delta G_f^\circ(Ag(s)) + \Delta G_f^\circ(e^-) - \Delta G_f^\circ(Ag^+(aq)) = -\Delta G_f^\circ(Ag^+(aq)) = -F\Delta E^\circ$   
 Therefore,  $\Delta G_f^\circ(Ag^+(aq)) = F\Delta E^\circ = 77.15 \text{ kJ/mol}$

13-2.  $Ag^+(aq) + 2 NH_3(aq) \rightarrow Ag(NH_3)_2^+(aq)$   
 $\Delta G^\circ = \Delta G_f^\circ(Ag(NH_3)_2^+(aq)) - \Delta G_f^\circ(Ag^+(aq)) - 2 \Delta G_f^\circ(NH_3(aq))$   
 $= -17.12 \text{ kJ} - 77.15 \text{ kJ} - (2)(-26.50) \text{ kJ} = -41.27 \text{ kJ}$   
 $\ln K_f = \frac{-\Delta G^\circ}{RT} = 16.65$                        $K_f = \frac{[Ag(NH_3)_2^+]}{[Ag^+][NH_3]^2} = e^{16.65} = 1.7 \times 10^7$

13-3.  $AgBr(s) \rightarrow Ag^+(aq) + Br^-(aq)$        $\Delta E^\circ = (0.0713 - 0.7996) \text{ V} = -0.7283 \text{ V}$   
 $\ln K_{sp} = \frac{-\Delta G^\circ}{RT} = \frac{nF\Delta E^\circ}{RT} = -28.17$   
 $K_{sp} = [Ag^+][Br^-] = e^{-28.347} = 4.8_9 \times 10^{-13}$

13-4. Let us assume  $[Ag^+] \ll [Ag(NH_3)_2^+]$ .



Initial	0.100	0	0
Change	-2S	+S	+S
Equilibrium	0.100 - 2S	S	S

$$K = \frac{S^2}{(0.1 - 2S)^2} = 8.31 \times 10^{-6} \rightarrow \frac{S}{(0.1 - 2S)} = 2.88 \times 10^{-3}$$

$$S = [Ag(NH_3)_2^+] = [Br^-] = 2.9 \times 10^{-4} \text{ M}$$

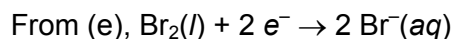
$$[Ag^+] = K_{sp}/[Br^-] = 1.7 \times 10^{-10} \text{ M} \ll [Ag(NH_3)_2^+]$$

Thus, the solubility of AgBr is  $2.9 \times 10^{-4} \text{ M}$

13-5.  $[Br^-] = K_{SP} / [Ag^+] = 4.89 \times 10^{-13} / 0.0600 = 8.15 \times 10^{-12}$

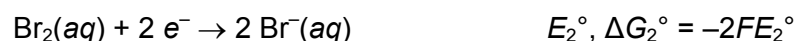
$$\begin{aligned} \Delta E^\circ &= \Delta E + \frac{RT}{nF} \ln \frac{[Br^-]^2 [H_3O^+]^2}{P_{H_2}} \\ &= 1.721 + \frac{0.0592}{2} \log_{10} \frac{(8.15 \times 10^{-12})^2 1^2}{1} = 1.065 \text{ V} \end{aligned}$$

13-6. In order to estimate the solubility of  $Br_2(aq)$ , we need to calculate the Gibbs free energy of the reaction:

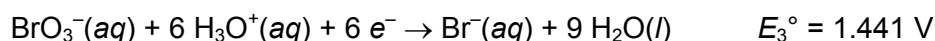


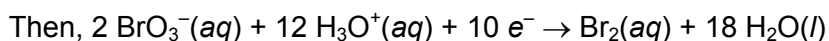
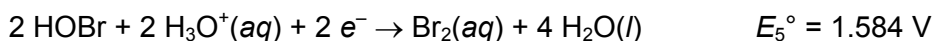
$$E_1^\circ = 1.065 \text{ V}, \Delta G_1^\circ = -2FE_1^\circ = -2.130F \text{ V}$$

Let us first calculate  $E_2^\circ$  for the half-cell reaction:

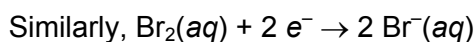


From the Latimer diagram,





$$E_6^\circ = (2 \times 4E_4^\circ + 2E_5^\circ)/10 = 1.5096 \text{ V}$$



$$E_2^\circ = (2 \times 6E_3^\circ - 10E_6^\circ)/2 = 1.098 \text{ V}$$

$$\text{(Note that } 6 \times E_3^\circ = 4 \times E_4^\circ + 1 \times E_5^\circ + 1 \times E_2^\circ)$$

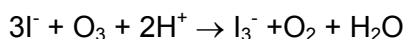
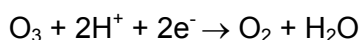
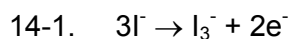
$$\text{Then, } \Delta G_2^\circ = -2\Delta E_2^\circ = -2.196F \text{ V}$$

$$\text{Finally, } \Delta G^\circ = \Delta G_1^\circ - \Delta G_2^\circ = 0.066F \text{ V} = 6368 \text{ J/mol}$$

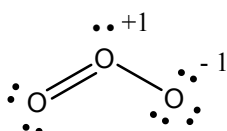
Therefore,

$$[\text{Br}_2(\text{aq})] = K = e^{\frac{-\Delta G^\circ}{RT}} = e^{-2.569} = 0.077 \text{ (M)}$$

#### Problem 14: Measuring the ozone level in air



14-2.



14-3. The absorbance is given by

$$A = -\log T = -\log(I_{\text{sample}}/I_{\text{blank}}) = \log(R_{\text{sample}}/R_{\text{blank}})$$

$$= \log(19.4 \text{ k}/12.1 \text{ k}) = 0.205$$

$$[\text{I}_3^-] = A / \epsilon b = 0.205 / (240,000 \text{ M}^{-1}\text{cm}^{-1})(1.1 \text{ cm}) = 7.76 \times 10^{-7} \text{ M}$$

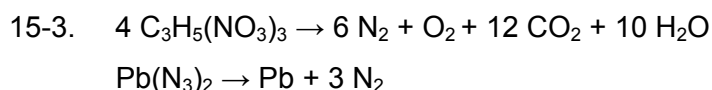
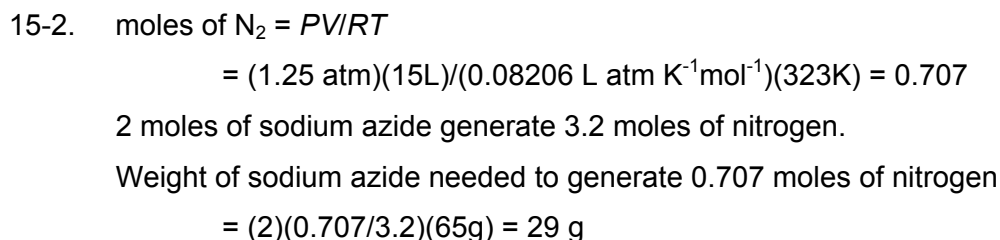
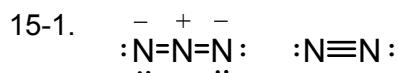
$$\text{Number of moles O}_3 = V_{\text{sample}} [\text{I}_3^-] = (0.01 \text{ L})(7.76 \times 10^{-7} \text{ mol/L}) = 7.76 \times 10^{-9} \text{ mol}$$

14-4. The number of moles of air sampled

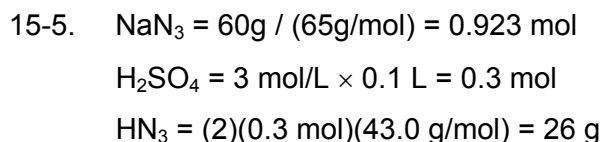
$$= PV/RT = P(t_{\text{sampling}} F)/RT$$

$$= (750 \text{ torr})(30 \text{ min})(0.250 \text{ L/min}) / (62.4 \text{ torr}\cdot\text{L mol}^{-1}\text{K}^{-1})(298 \text{ K}) = 0.302 \text{ mol}$$

$$\text{The concentration of O}_3 \text{ in ppb} = (7.76 \times 10^{-9} \text{ mol} / 0.302 \text{ mol}) \times 10^9 = 25.7$$

**Problem 15: Lifesaving chemistry of the airbag**

In all three reactions, the reactants are solid or liquid with small volume. A large volume of nitrogen gas is produced. Nitroglycerin produces other gases. The nitrogen molecule has a triple bond and is very stable. Thus, the reactions are highly exothermic, so that gases produced expand rapidly.

**Problem 16: Catalysis for the synthesis of ammonia**

16-1  $\Delta S^\circ = (2)(192.5) - (191.6 + 3 \times 130.7) = -198.7 \text{ J/(K}\cdot\text{mol)}$

The reaction must be exothermic and produce enough heat to increase the entropy of the surroundings and thereby offset the decrease in system entropy.

16-2 Combination of hydrogen with a more electronegative element will be more exothermic.

$\text{H}_2\text{O(g)}: -241.82 \text{ kJ/mol}$

$\text{HF(g)}: -271.1 \text{ kJ/mol}$



$\text{NH}_3(\text{g})$ : - 46.11 kJ/mol

16-3.  $\Delta S_{\text{tot}} = \Delta S_{\text{sys}} + \Delta S_{\text{sur}} = \Delta S_{\text{sys}} - \Delta H_{\text{sys}}/T$   
 $= 198.7 \text{ J/K} + (92.22 \times 10^3 \text{ J}/298 \text{ K}) = + 110 \text{ J/K}$

16-4.  $\text{NH}_3(\text{g})$ : - 46.11 kJ/mol

$$k_1 = A \exp(-E_a/RT) = 10^{13} \exp[-940 \times 10^3 / (8.3145 \times 1073)] = 1.74 \times 10^{-33} \text{ sec}^{-1}$$

$$k_2 = A \exp(-E_a/RT) = 10^{13} \exp[-470 \times 10^3 / (8.3145 \times 1073)] = 1.32 \times 10^{-10} \text{ sec}^{-1}$$

$$k_2/k_1 = 7.6 \times 10^{22}$$

16-5. mass of cube =  $7.86 \text{ g/cm}^3 \times (10^{-4} \text{ cm})^3 = 7.86 \times 10^{-15} \text{ kg}$

$$\text{number of cubes in 1 kg} = 1 \text{ kg} / (7.86 \times 10^{-15} \text{ kg}) = 1.27 \times 10^{14}$$

$$\text{surface area of Fe powder} = 6 \times 10^{-12} \text{ m}^2 \times 1.27 \times 10^{14} = 763 \text{ m}^2$$

$$\text{area for N}_2 \text{ adsorption} = 0.16 \times 10^{-18} \text{ m}^2$$

$$N = \text{area of Fe powder} / \text{area for N}_2 = 4.77 \times 10^{21} = 7.92 \times 10^{-3} \text{ mole}$$

16-6.  $1 \text{ kg} / (0.5 \text{ kg/mole}) = 2 \text{ mole} = 1.20 \times 10^{24}$

16-7.  $8 \times 30.5 \text{ kJ/mole} = 244 \text{ kJ}$

$E(\text{nitrogenase}) < E(\text{chemical industry})$

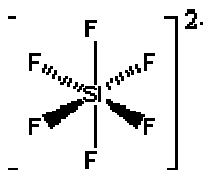
### Problem 17: From sand to semiconductors

17-1. Si:  $1/8 \times 8 + 1/2 \times 6 + 1 \times 4 = 8$

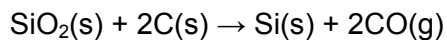
O:  $1 \times 16 = 16$

17-2.  $\text{sp}^3$ ;  $109.5^\circ$

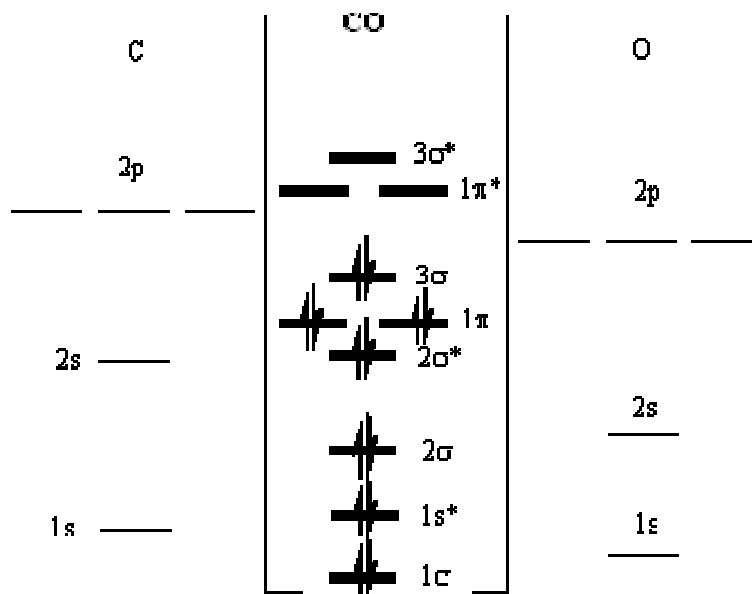
17-3. octahedral:



- 17-4. Since Lewis structure of the gas shows the formal charges, it should not be  $\text{O}=\text{C}=\text{O}$ , but  $:\text{C}\equiv\text{O}:$  where C has the formal charge of -1 and O has the formal charge of +1. Therefore, the balanced equation for the reaction is

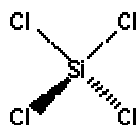


- 17-5.

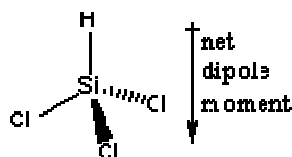


- 17-6.  $\text{Si}(\text{s}) + 2\text{Cl}_2(\text{g}) \rightarrow \text{SiCl}_4(\text{l})$  : from the *Merck Index*  
Schenk in *Handbook of Preparative Inorganic Chemistry* Vol. 1, G. Brauer, Ed.  
(Academic Press, New York, 2nd ed., 1963) pp 682-683.

- 17-7. Tetrahedral



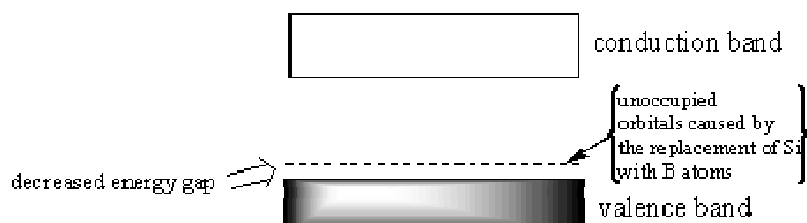
- 17-8.  $\text{C} = \text{SiHCl}_3$ , polar



- 17-9.  $(1 \text{ g}/32.066 \text{ g/mol}) \times 0.1 \times 10^{-9} \times 6.02 \times 10^{23} = 1.9 \times 10^{12}$

17-10. In a Si wafer doped with B atoms, holes exist that neighboring electrons can move into, thus causing electrical conductivity. Therefore, holes are the charge carriers. This kind of doped-semiconductor is the p-type semiconductor.

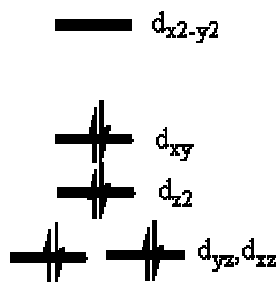
17-11.



### Problem 18: Self-assembly

18-1. square planar

18-2.  $\text{Ni}^{2+}$ ,  $d^8$ , square planar, diamagnetic



18-3. a long alkyl side chain:  $-\text{C}_{16}\text{H}_{33}$ .

18-4. hydrophobicity due to the long alkyl chains

18-5. bond a

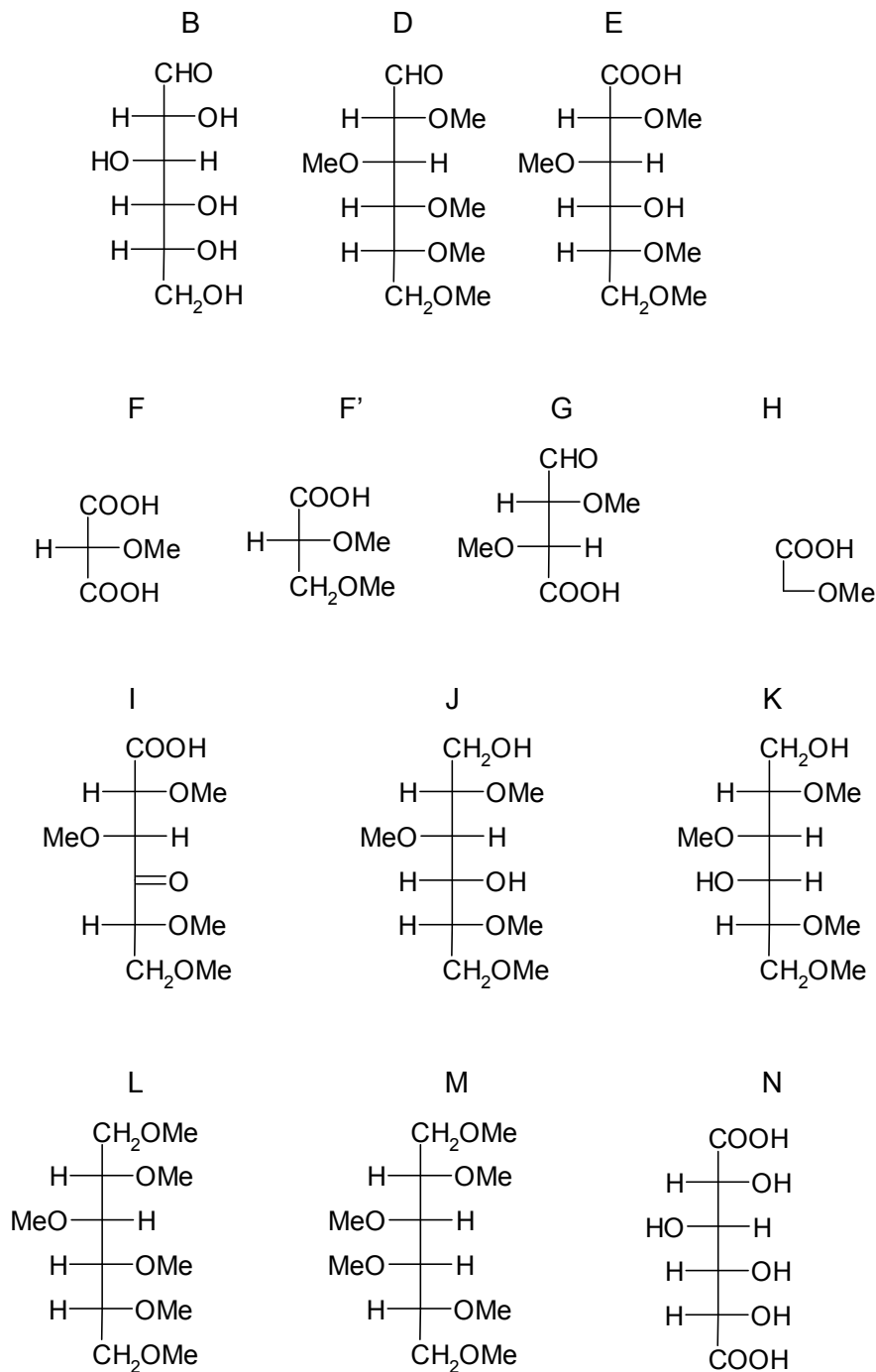
18-6. bonds b and d are shortened upon reduction.

18-7. coordination number of 6

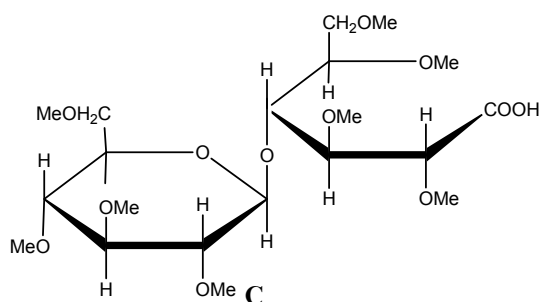
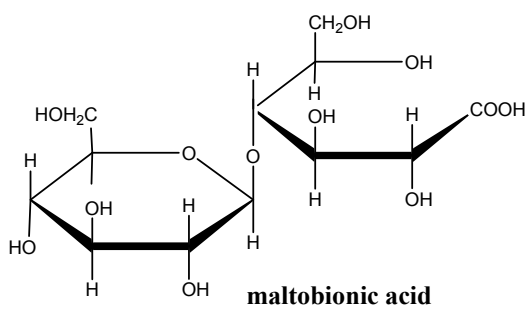
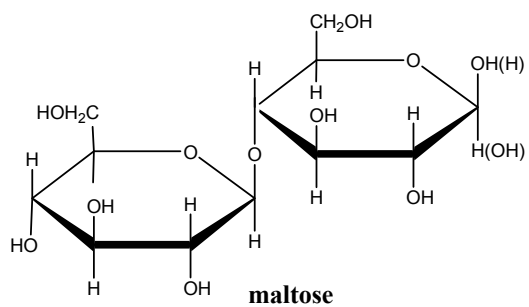
18-8.  $\pi$ - $\pi$  stacking interactions

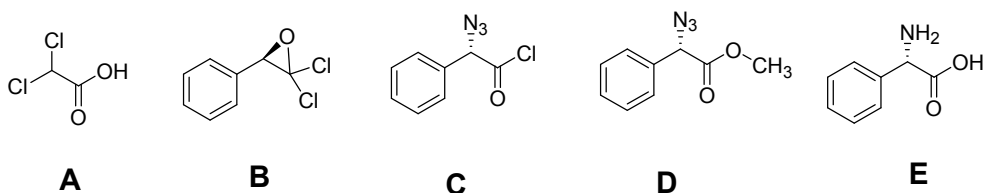
### Problem 19: Stereochemistry (Organic synthesis – 1)

19-1.

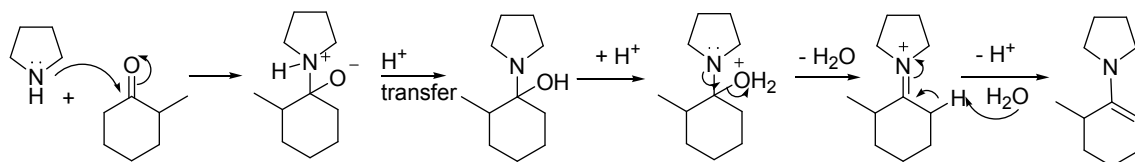


19-2.



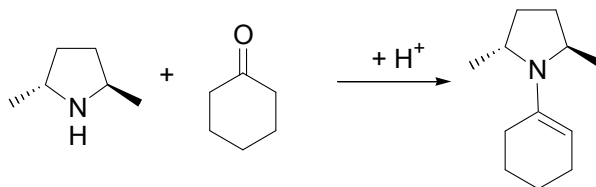
**Problem 20: Total synthesis (Organic synthesis – 2)**configuration : **S****Problem 21: Enamine chemistry (Organic synthesis – 3)**

21-1.



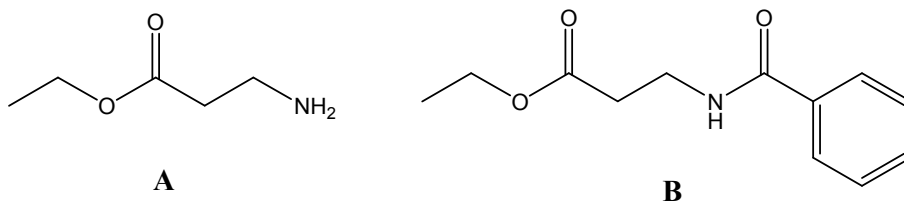
21-2. Normally, acid catalyzes the enamine formation as shown in 21-1. However, if too much acid is present, the basic amine (nucleophile) is completely protonated so the initial nucleophilic addition step cannot occur.

21-3. An enamine prepared from a single enantiomer of the chiral secondary amine is chiral, and thus the Michael addition reaction can proceed from only one side of enamine to yield a single enantiomeric product.

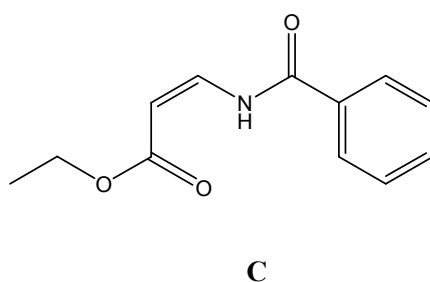


**Problem 22: Oxidation and reduction in organic synthesis**

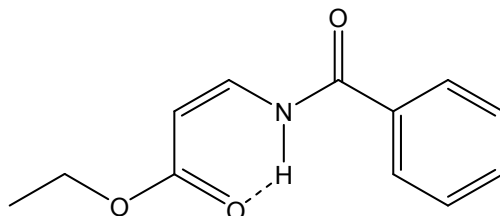
22-1.



22-2.



22-3. The cis-conformation of the olefin allows the strong hydrogen bonding between the proton of the amide and the carbonyl oxygen of the ester as shown in the following structure.



The strong hydrogen bonding moved the chemical shift of the amide proton toward further down-field.

**Problem 23: Antifreeze proteins**

23-1. For freezing point depression,  $\Delta T = -K_f m$

The molal concentration  $m$  is obtained by

$$-20 = -1.86 m,$$

$$m = 10.75 \text{ mol/kg}$$

The weight of the glycerol in 1 kg of water is

$$w = m \times MW = 10.75 \times 92 = 989 \text{ kg.}$$

Therefore, glycerol would be about 50 % by weight.

This is a ridiculously large number indicating that something else is also required to avoid freezing.

Osmotic pressure is obtained from the van't Hoff equation,  $\pi = cRT$ .

Assuming that the molar concentration  $c$  is approximately the same as the molal concentration obtained above,

$$\text{Osmotic pressure} = 10.75 \times 0.082 \times (273 - 20) = 223 \text{ atm}$$

The osmotic pressure is extremely high, and the organism may not be stable.

23-2. From Figure 1, the glycerol content in January is

$$2500 \text{ } \mu\text{mol/g} = 2.5 \text{ mol/kg} = (230 \text{ g glycerol}) / (1 \text{ kg water}).$$

Therefore, the glycerol fraction is 18.7 % of total weight.

Freezing point depression at this concentration is

$$-2.5 \times 1.86 = -4.7^\circ\text{C},$$

which is significantly higher than the temperature in January.

23-3. Threonine and aspartate side chains can contact each other through their oxygen and hydrogen groups to form stable hydrogen bonds. The hydrogen bonds of these side chains might preferably interact with water molecules of the ice particle surfaces, thus inhibiting ice crystal growth.



**Problem 24: The human body**

- 24-1. average atomic weight of three atoms in a water molecule =  $18/3 = 6$   
 average atomic weight of atoms in other molecules is about the same.  
 For example, consider carbohydrate,  $C(H_2O)$ .  $28/4 = 7$   
 So, let's assume that the human body is composed of only water.  
 60 kg of water = 10,000 moles of atoms =  $6 \times 10^{27}$  atoms or about  $10^{28}$  atoms
- 24-2. Assume that the density of the human body is  $1 \text{ g/cm}^3$ .  
 volume of body =  $6 \times 10^{-2} \text{ m}^3$   
 volume of a cell =  $6 \times 10^{-16} \text{ m}^3$   
 length of a cell =  $8 \times 10^{-6} \text{ m}$  (about 10 micrometers)
- 24-3. number of atoms in a cell =  $10^{28} / 10^{14} = 10^{14}$   
 volume per atom in a cell =  $6 \times 10^{-16} \text{ m}^3 / 10^{14} = 6 \times 10^{-30} \text{ m}^3$   
 distance between two atomic nuclei =  $2 \times 10^{-10} \text{ m} = 2 \text{ Angstroms}$
- 24-4. volume of a mole of water =  $18 \times 10^{-6} \text{ m}^3$   
 average volume occupied by a water molecule =  $3 \times 10^{-29} \text{ m}^3$   
 distance between center of mass of two water molecules  
 =  $3 \times 10^{-10} \text{ m} = 3 \text{ Angstroms}$
- 24-5. volume of a mole of water =  $18 \times 10^{-6} \text{ m}^3$   
 number of atoms in a mole of water =  $18 \times 10^{23}$   
 average volume occupied by an atom in water =  $10^{-29} \text{ m}^3$   
 average distance between atomic nuclei in water  
 =  $2 \times 10^{-10} \text{ m} = 2 \text{ Angstroms}$

**Problem 25: Hemoglobin**

- 25-1. 150 g hemoglobin in 1 L  
 $150 \text{ g}/67,000 \text{ g mol}^{-1} = 0.0022 \text{ mol}$  0.0022 M
- 25-2. volume of a mole of air =  $22.4 \times 10^{-3} \text{ m}^3$   
 number of oxygen molecules in above volume  
 $= (6.02 \times 10^{23})(0.21) = 1.26 \times 10^{23}$   
 volume of air per oxygen molecule  
 $= (22.4 \times 10^{-3} \text{ m}^3)/(1.26 \times 10^{23}) = 1.78 \times 10^{-25} \text{ m}^3$   
 average distance between oxygen molecules =  $5.6 \times 10^{-9} \text{ m}$
- 25-3. solubility =  $(1.3 \times 10^{-3} \text{ mol L}^{-1} \text{ atm}^{-1})(0.21 \text{ atm}) = 2.7 \times 10^{-4} \text{ mol L}^{-1}$   
 number of oxygen molecules in a liter of water  
 $= (6 \times 10^{23} \text{ mol}^{-1})(2.7 \times 10^{-4} \text{ mol}) = 1.6 \times 10^{20}$   
 volume of water per oxygen molecule  
 $= (1 \times 10^{-3} \text{ m}^3)/(1.6 \times 10^{20}) = 6.3 \times 10^{-24} \text{ m}^3$   
 average distance between oxygen molecules =  $1.8 \times 10^{-8} \text{ m}$
- 25-4. number of oxygen molecules in 1 L of blood  
 $= (4)(0.0022)(6 \times 10^{23}) = 5.3 \times 10^{21}$   
 volume of blood per oxygen molecule  
 $= 10^{-3} \text{ m}^3 / 5.3 \times 10^{21} = 1.9 \times 10^{-25} \text{ m}^3$   
 distance between oxygen molecules  
 $= 5.7 \times 10^{-9} \text{ m}$
- 25-5. The average molecular weight of amino acids is about 130.  
 Water is removed upon peptide bond formation.  
 $67,000/(130 - 18) = 600$  amino acid residues  
 Actually hemoglobin has two alpha and two beta chains, each of which consists of 141 residues.
- 25-6. All life-forms on earth use 20 common amino acids.

25-7. Trypsin hydrolyzes after 2 amino acid residues (arginine and lysine) out of 20 different kinds of amino acids. So, on average the enzyme breaks every 10<sup>th</sup> peptide bond.

The number of amino acid residues in an average tryptic peptide = 20/2 = 10

25-8. Consider removal of water in the peptide bond formation.

$(130 - 18) \times 10 + 18 = 1,140 = \text{about } 1,000$

### Problem 26: Mass spectrometry of hemoglobin

26-1. osmotic pressure (freezing point depression is too small, mass spectrometry is not available)

26-2. For a singly charged protein ion (67,435 Da)

electrical energy =  $eV = (1.60218 \times 10^{-19} \text{ C})(2.0000 \times 10^4 \text{ V}) = 3.20436 \times 10^{-15} \text{ J}$

26-3.  $mv^2/2 = \text{electrical energy}$

$m = (2)(\text{electrical energy})/v^2$

$= (2)(3.20436 \times 10^{-15} \text{ J})/(1.0000 \text{ m}/1.3219 \times 10^{-4} \text{ s})^2 = 1.11987 \times 10^{-22} \text{ kg}$

$MW \text{ of } [M+H]^+ = (1.11987 \times 10^{-22} \text{ kg})(6.0221 \times 10^{23}) = 67.440 \text{ kg}$

$MW \text{ of hemoglobin} = 67,440 - 1 = 67,439$

mass accuracy =  $67,439/67,434 = 1.000074$                       74 ppm

26-4. volume of collision cylinder =  $\pi d^2 v$

number of molecules in unit volume:  $N/V = PN_0/RT$

collision/sec = (volume of collision cylinder)(molecules/unit volume)

$= (\pi d^2 v)(PN_0/RT)$

time between collisions =  $1/[(\pi d^2 v)(PN_0/RT)]$

mean free path = speed/time between collisions

$= v / [(\pi d^2 v)(PN_0/RT)] = 1 \text{ m}$

$P = (RT/N_0)/[(\pi d^2)(1 \text{ m})]$

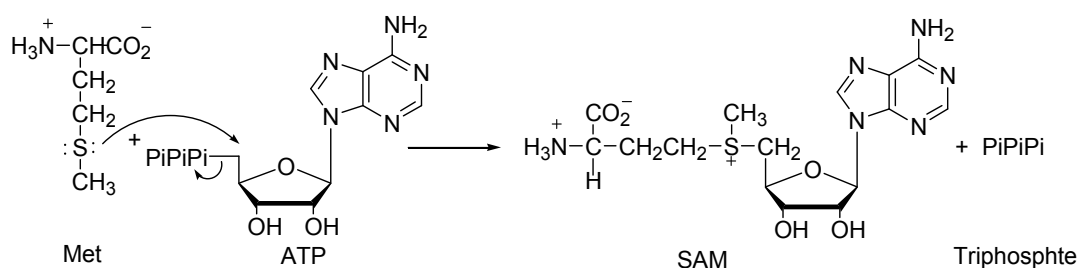
$= (8.314 \text{ J mol}^{-1} \text{ K}^{-1})(298 \text{ K})/[(6.02 \times 10^{23} \text{ mol}^{-1})(3.14)(2 \times 10^{-10} \text{ m})^2(1 \text{ m})]$

$= 3.3 \times 10^{-2} \text{ Pa} = 3.2 \times 10^{-7} \text{ atm}$

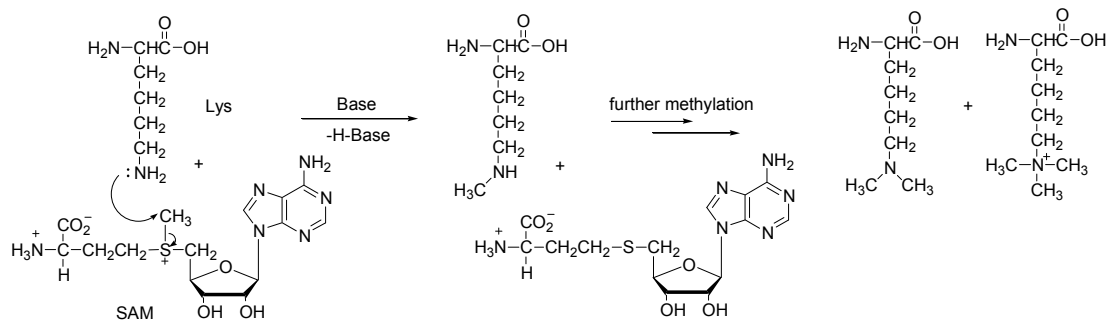
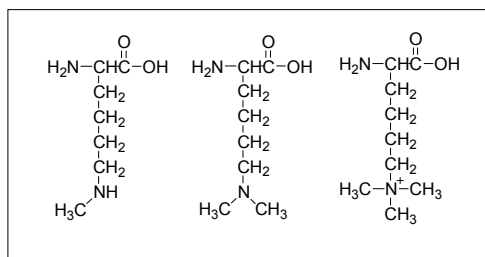
**Problem 27: Post-translational modification**

27-1. Lys (K) and Arg (R) provide plausible methylation sites at their side chains, because they can accept more than one methyl groups. Other amino acids side chains with oxygen nucleophile can hold only one methylation.

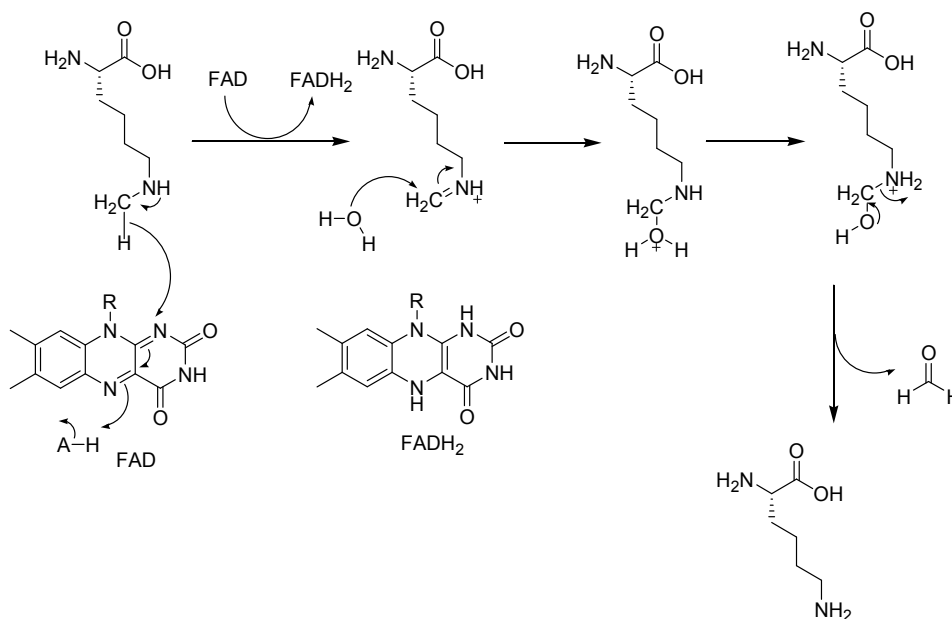
27-2. Triphosphate group is a good leaving group and sulfur is a good nucleophile. Sulfur of methionine undergoes S<sub>N</sub>2 type reaction with ATP with triphosphate as the leaving group to form SAM.



27-3.



27-4.

**Problem 28: Transition state in enzymatic reactions**

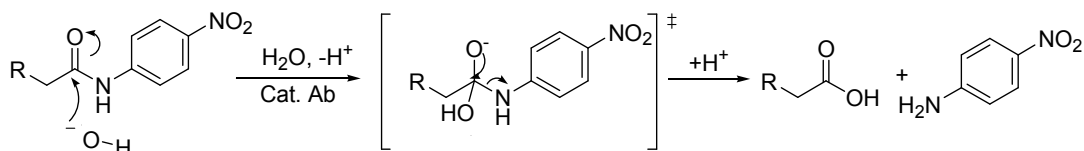
28-1. The reduced energy of the transition state can be calculated by comparing  $\Delta G^\circ$  ( $\Delta G^\circ = -RT \ln K_{eq}$ ) values between  $K_D$  of selected antibody and normal antibody).

$$\begin{aligned} \Delta G^\circ &= (-RT \ln K_{D, \text{selected}}) - (-RT \ln K_{D, \text{normal}}) = -RT(\ln K_{D, \text{selected}} - \ln K_{D, \text{normal}}) \\ &= -8.32 \times 310 \times \ln(10^{-13}/10^{-6}) = 41.6 \text{ kJ/mol} \end{aligned}$$

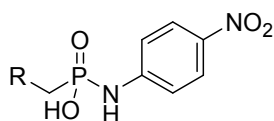
28-2.  $k_{cat}/k_{uncat} = \exp(E_{uncat} - E_{cat}/RT)$  by Arrhenius equation ( $k = A \exp(-E_a/RT)$ )

$$k_{cat}/k_{uncat} = \exp(41,600/8.32 \times 310) = 1 \times 10^7 \quad (\text{ratio of } K_D \text{ above})$$

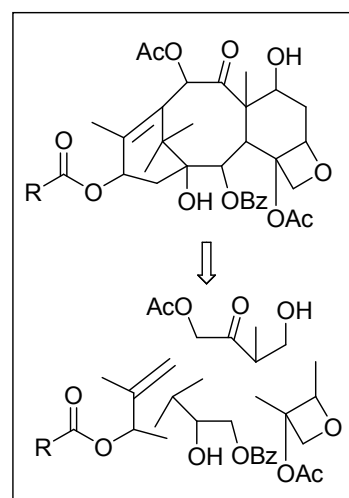
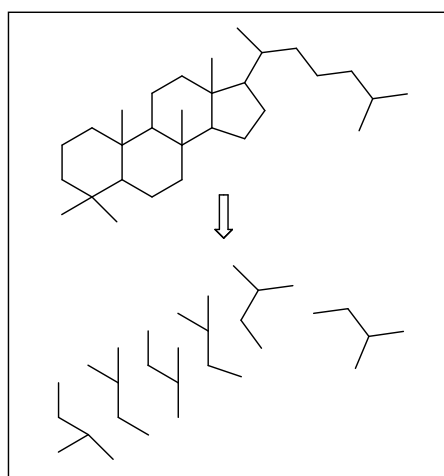
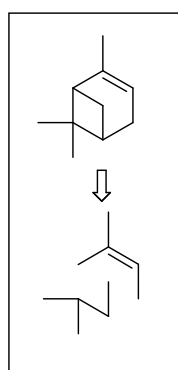
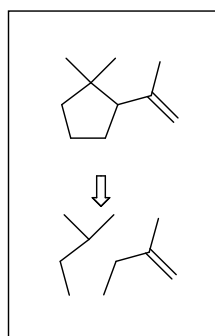
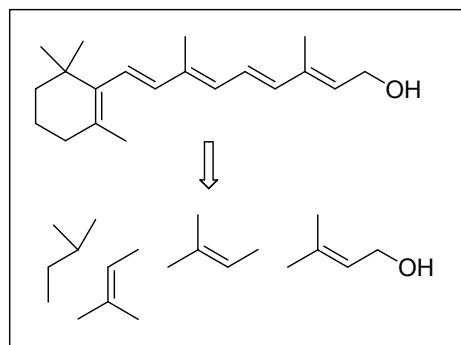
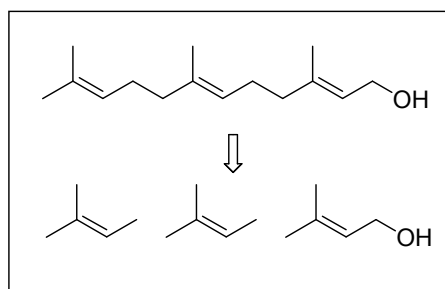
28-3.

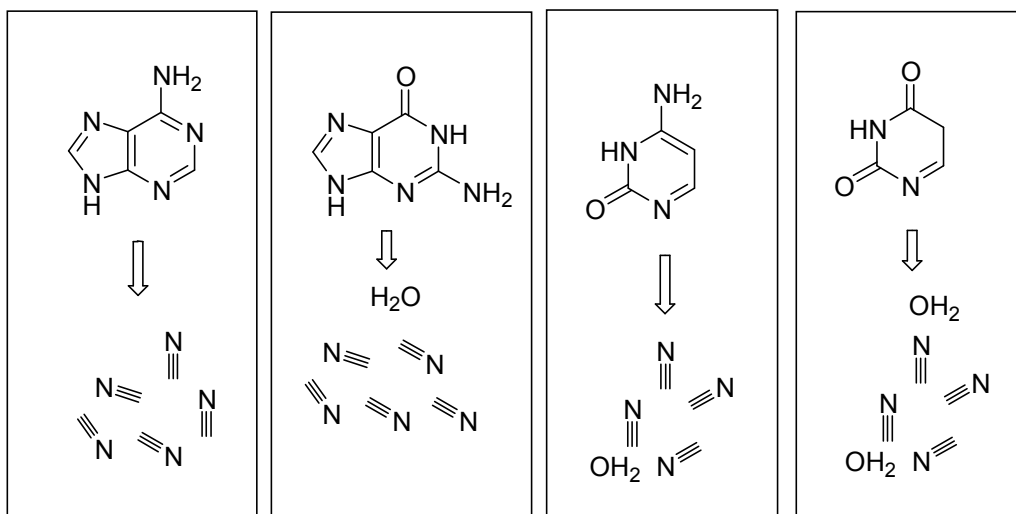
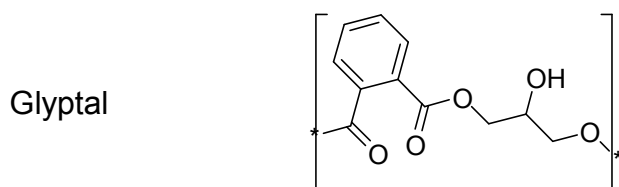
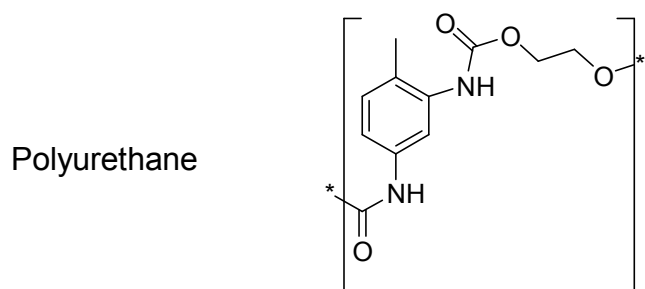
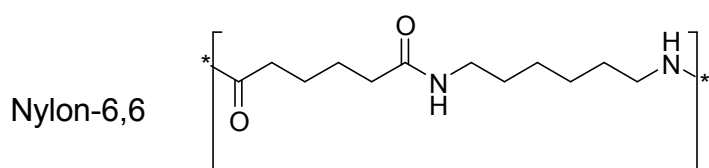


28-4.



### Problem 29: Nature's building blocks





**Problem 30: True or false**

True: 2, 3, 7, 8, 9, 11

False: 1, 4, 5, 6, 10, 12